



# A site index model for Norway spruce in Bavaria

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ZENTRUM WALD FORST HOLZ  
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# Structure

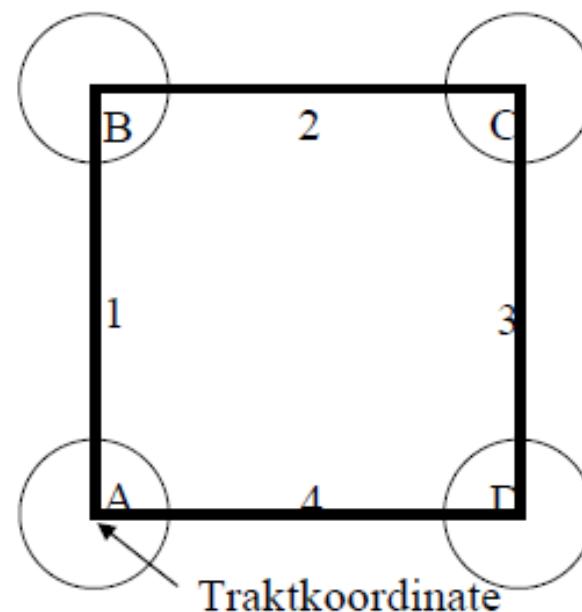
- Aims
- Database
- Height-diameter model
- Diameter-age model
- Prediction of site index
- Alternative approaches

# Aims

- Investigating the relationship between growth and site -> statistical model
- Site index (height at age 100) to compare site productivity
- Regionalisation -> maps for Bavaria
- Predictions for changing environmental conditions

# Data

- Data of the National Forest Inventories BWI 1 (1987) and BWI 2 (2002): height, BHD (diameter at breast height), age...
- Environmental data with high resolution (water balance, physical and chemical soil variables, monthly means of climatic variables, relief parameters)
- Regionalised daily surfaces of climatic variables (temperature, precipitation, evaporation)



# Height-Diameter-Model

- Based on an approach of Albert & Schmidt

(Albert, Matthias; Schmidt, Matthias (2009): Ein longitudinales Höhen-Durchmesser-Modell für Fichte in Deutschland, Tagungsband der Jahrestagung der Sektion Ertragskunde im DVFFA, S. 69-82 )

- Basis: Korf function

$$\ln(\text{height}) = A - B \cdot BHD^{-C}$$

- modification

$$\ln(\text{height}) = A - B \cdot xBHD$$

$$xBHD = \frac{(BHD + \lambda)^{-C} - (30 + \lambda)^{-C}}{(10 + \lambda)^{-C} - (30 + \lambda)^{-C}}$$

-> biological interpretation and reduction of correlation between parameters

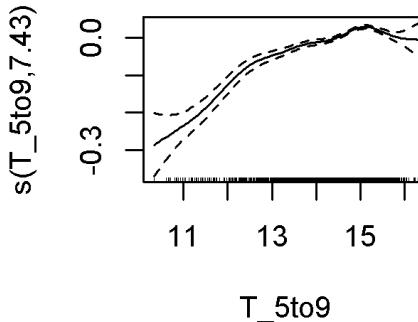
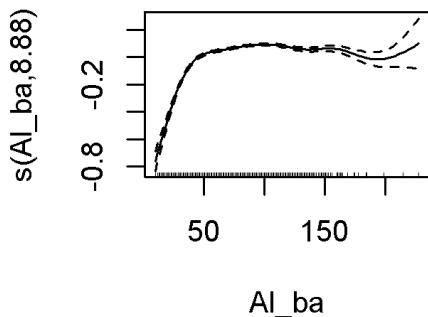
- A: expected value for  $\ln(\text{height})$  for trees with a diameter of 30 cm
- B: expected difference between  $\ln(\text{height})$  of trees with a diameter of 30 cm and trees with a diameter of 10 cm

# Height-Diameter-Model

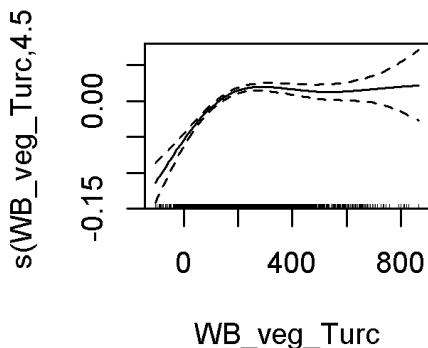
- Linearisation of the Korf function
  - 4 parameters are too many
  - direct application of GAM-method on the parameters
- Iterative identification of the optimal combination for  $\lambda$  and C in a GAM:  
 $\text{gam}(\log(\text{height}) \sim s(\text{age}) + te(x,y) + s(\text{elevation}) + xBhd + \text{age}:xBhd + \text{elevation}:xBhd)$
- Selection criterion: BIC  
 $\lambda = 6.6$  and  $C = 1.535$
- -> linear function with two parameters A and B  
 $\ln(\text{height}) = A - B \cdot xBHD$

# Effect of environmental variables on the parameter A of the Korf function

- $\text{gam}(\text{Höhe} \sim s(\text{Al}_\text{ba}) + s(\text{T}_\text{5to9}) + s(\text{WB}_\text{veg_Turc}) + \text{xBHD} + \text{Al}_\text{ba} : \text{xBHD} + \text{T}_\text{5to9} : \text{xBHD}, \text{data} = \text{Fichte}, \text{family} = \text{gaussian}(\text{link} = \text{log}))$



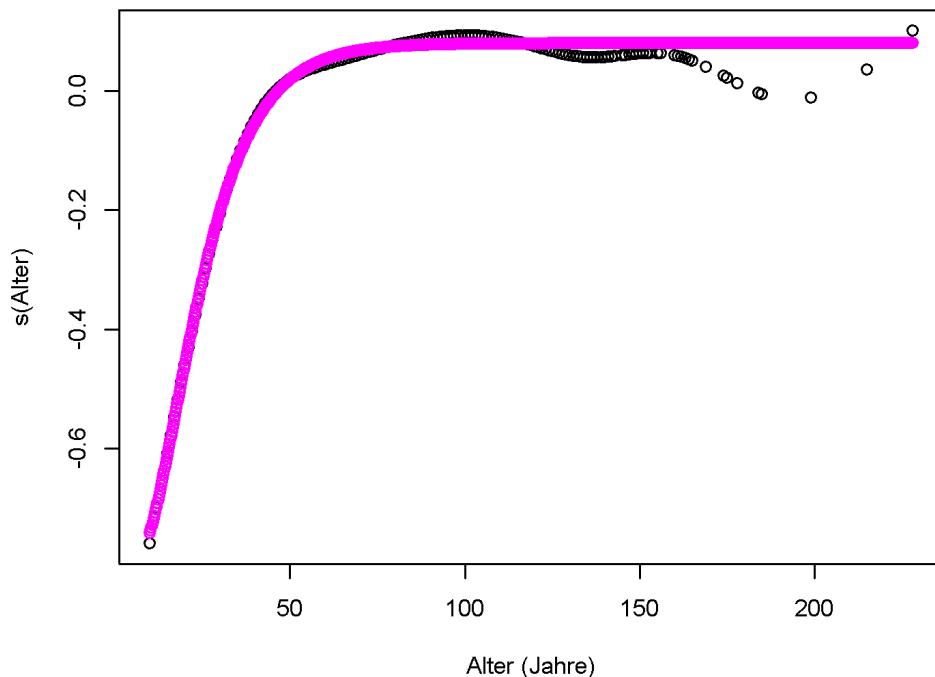
BIC = 25949.08  
GCV = 8.5293



Al<sub>ba</sub>: Alter  
T<sub>5to9</sub>: mittlere Temperatur Mai bis September  
WB<sub>veg\_Turc</sub>: Wasserbilanz während der  
Vegetationsperiode  
xBHD: modifizierter BHD

# Replacing smooth terms by parametric functions

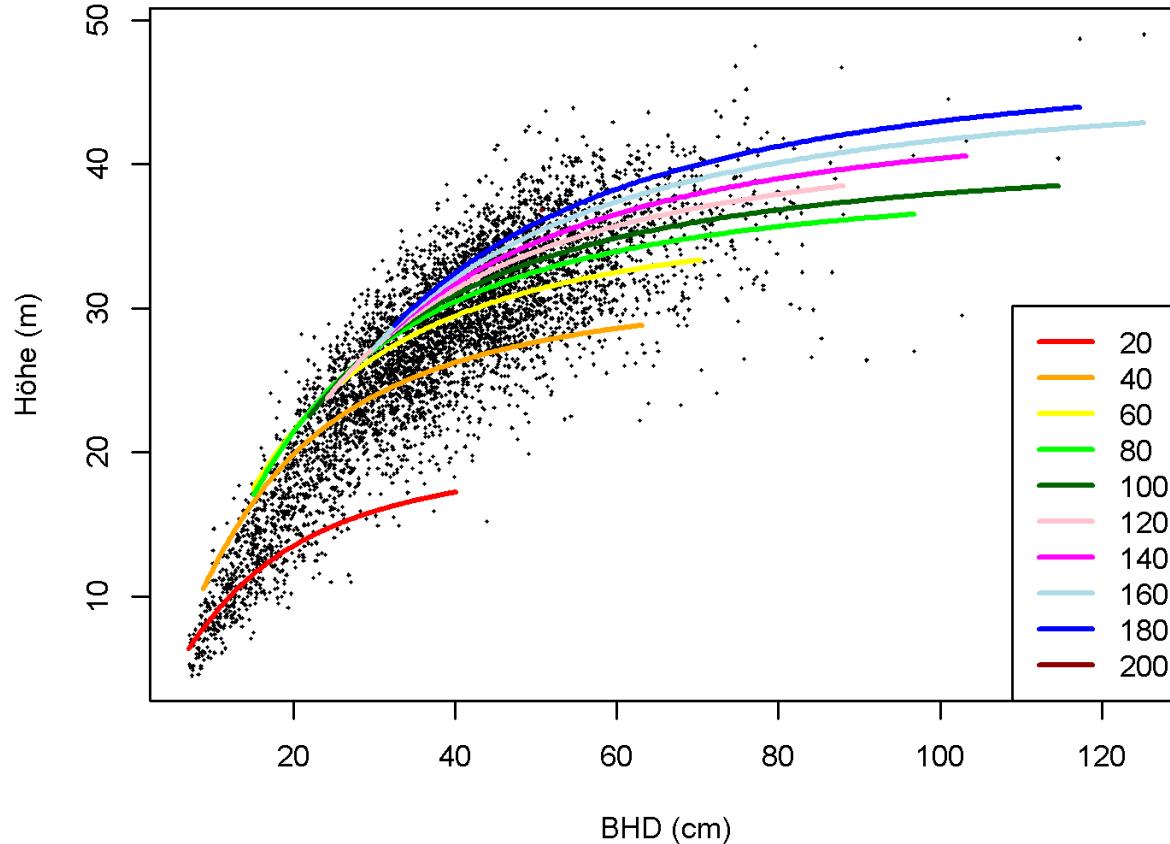
- glm\_rep <- glm(Hoehe ~ I((1 - exp(-0.08311921\*Al\_ba))^4.145161) + I(0.3814\*T\_5to9 + -0.01233\*T\_5to9^2) + I(0.02306-(0.07282 \* exp(-0.008566\*WB\_veg\_Turc))) + xBhd + Al\_ba:xBhd + T\_5to9:xBhd, data = Fichte, family = gaussian(link = log))



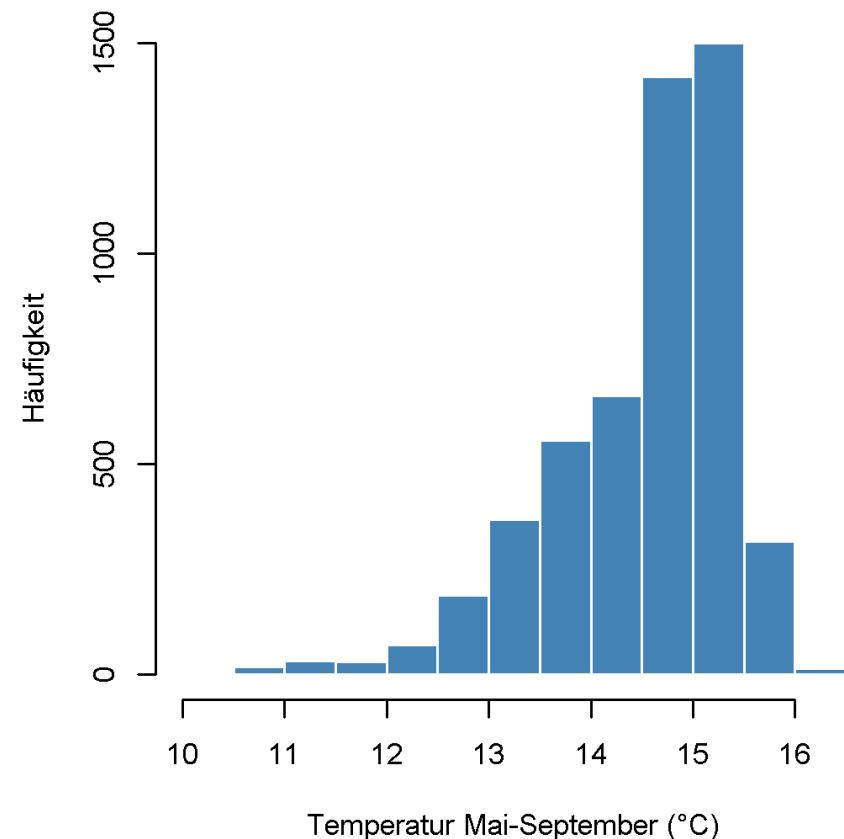
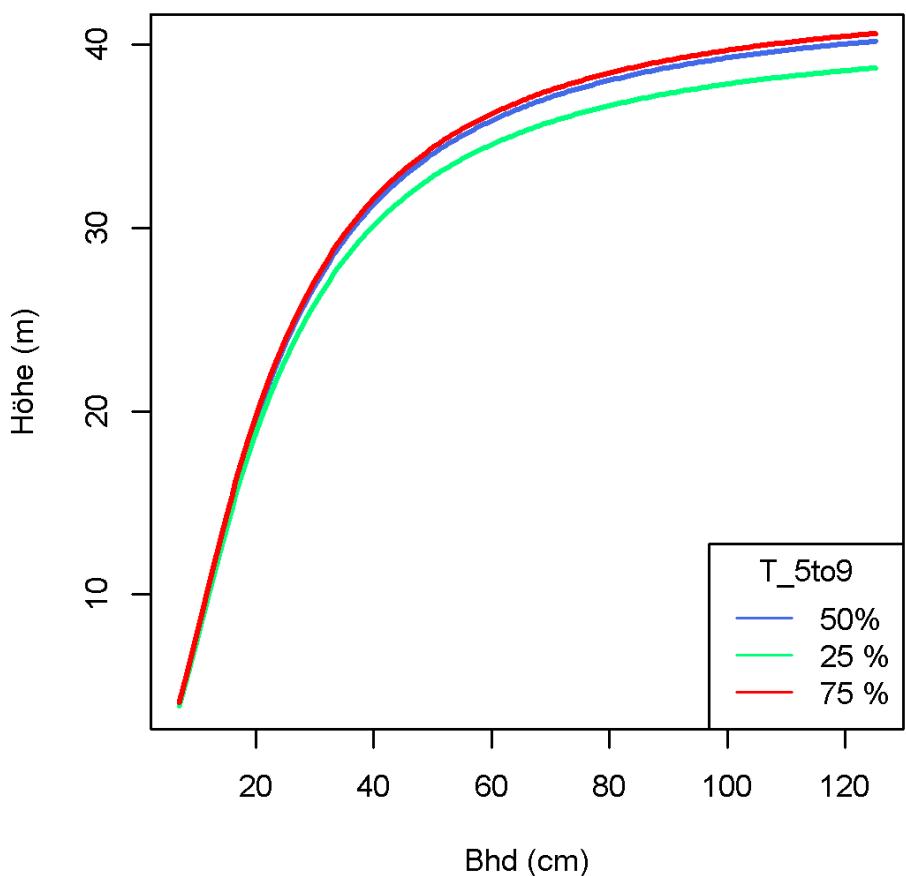
# Influence of diameter, age and environment

- A model with diameter and/or age alone already explains a great part of the variance
  - `gam1 <- gam(log(height) ~ s(xBhd))`  $R^2$  86 %
  - `gam2 <- gam(log(height) ~ s(Al_ba))`  $R^2$  80 %
  - `gam3 <- gam(log(height) ~ s(Al_ba) + xBhd + Al_ba:xBhd)`  $R^2$  88.9 %
  - Selected GAM with environmental variables  $R^2$  89.8 %

# Effect of age on height-diameter-model



# Effect of temperature on height-diameter-model



# Determination of Site Index

$$\ln(\text{height}) = A + f(\text{age}) + f(\text{temperature}) + f(\text{water balance}) \\ - (B + \beta_1 \cdot \text{age} + \beta_2 \cdot \text{temperature}) * xBHD$$

- Age = 100
- Diameter at age 100
  - Diameter at age 100 has to be predicted -> Diameter-Age-Model
  - Site specific: a tree has a bigger diameter at a favourable site than at an unfavourable site under otherwise equal conditions

# Diameter-Age-Model

- Based on an approach of Albert & Schmidt (NW-FVA)
- Basis: Bertalanffy function as a nonlinear mixed model (nlme)
- Modified version

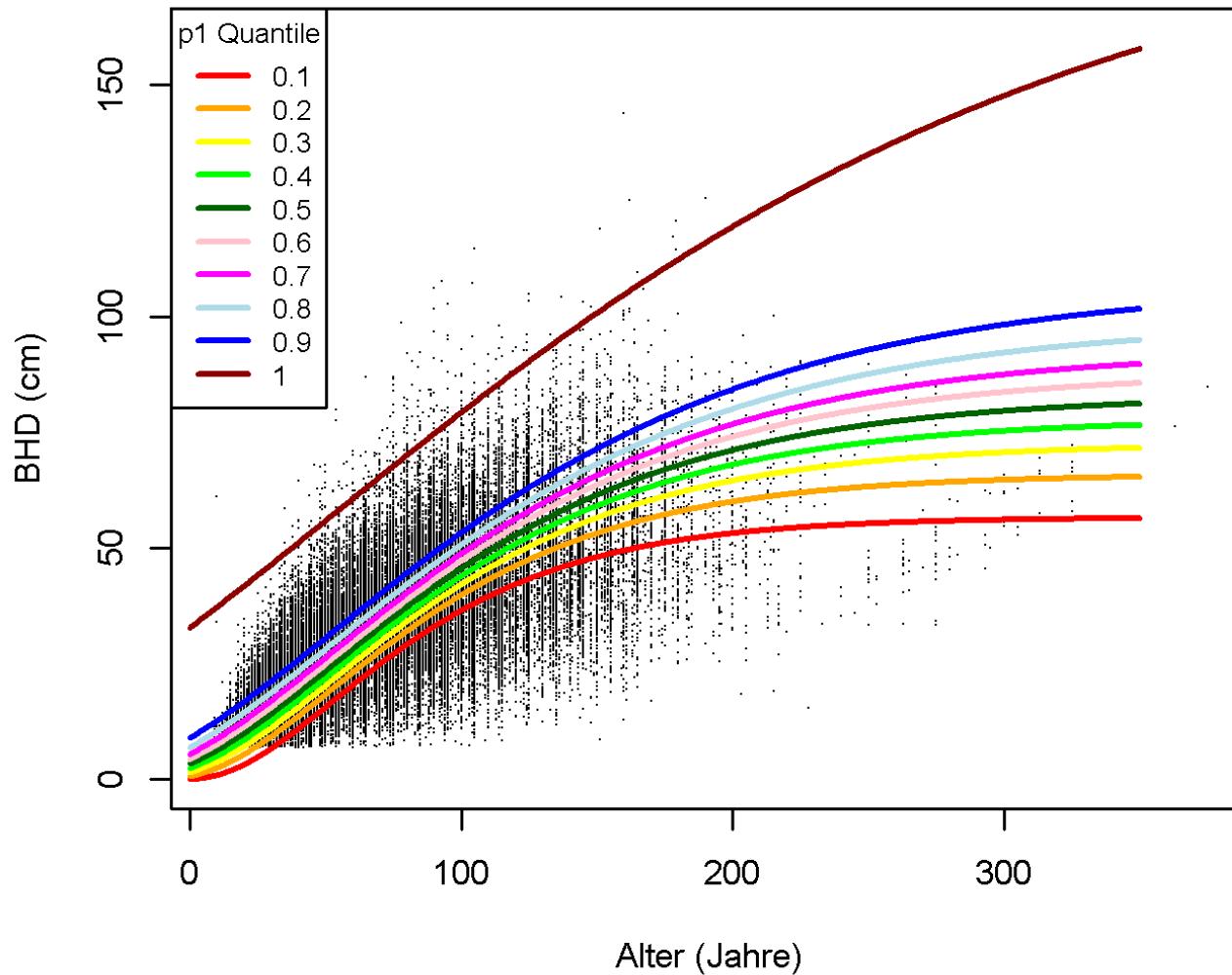
$$BHD_{ijk} = p_{1i} \cdot \left(1 - \frac{1}{3} \cdot e^{\left(\frac{p_3}{p_{1i}} \cdot (p_2 - Alter_{ijk}) \cdot \frac{9}{4}\right)}\right)^3$$

$p_1$ : Asymptote (cm)

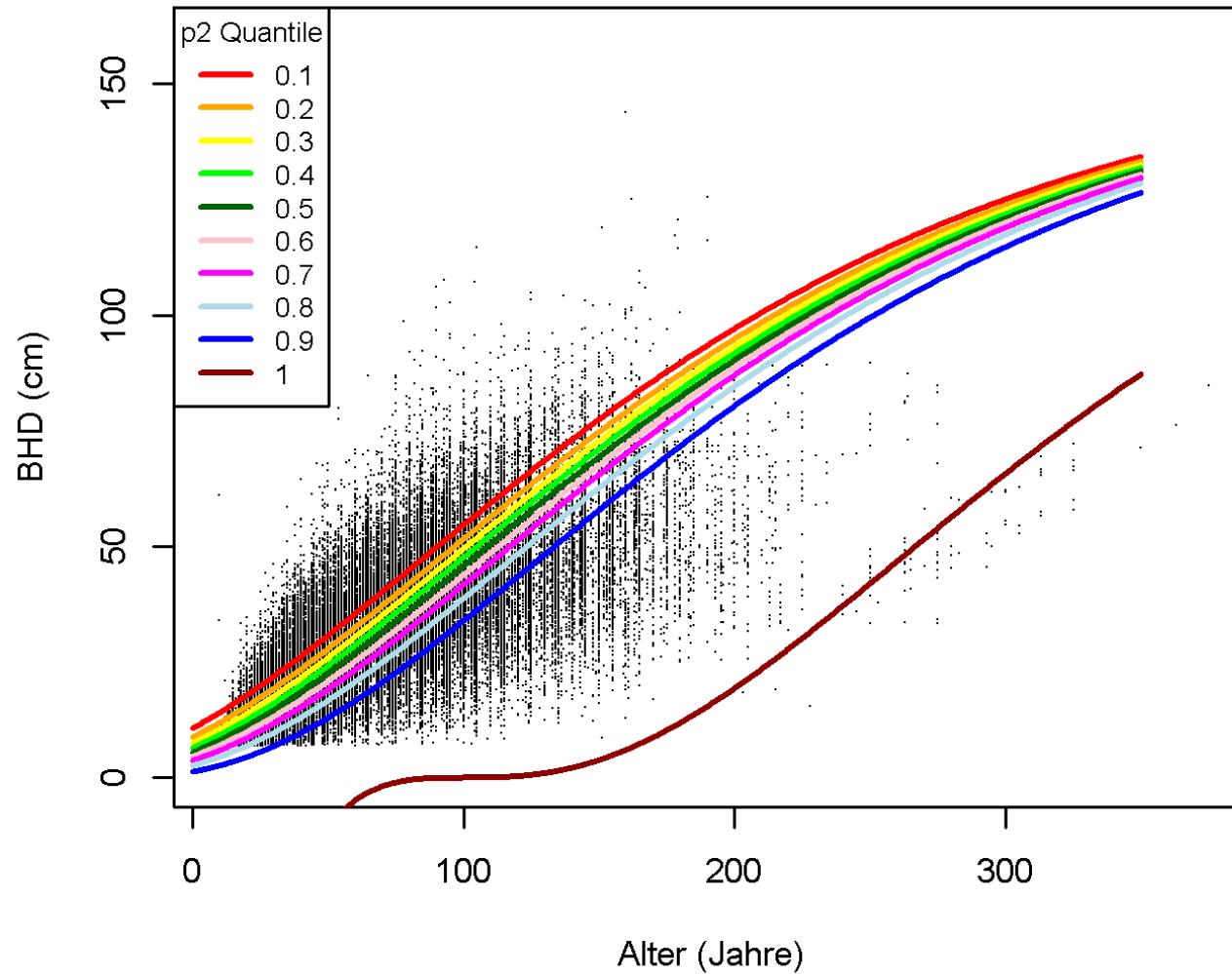
$p_2$ : point in time of maximum diameter growth (a)

$p_3$ : maximum diameter growth (cm/a)

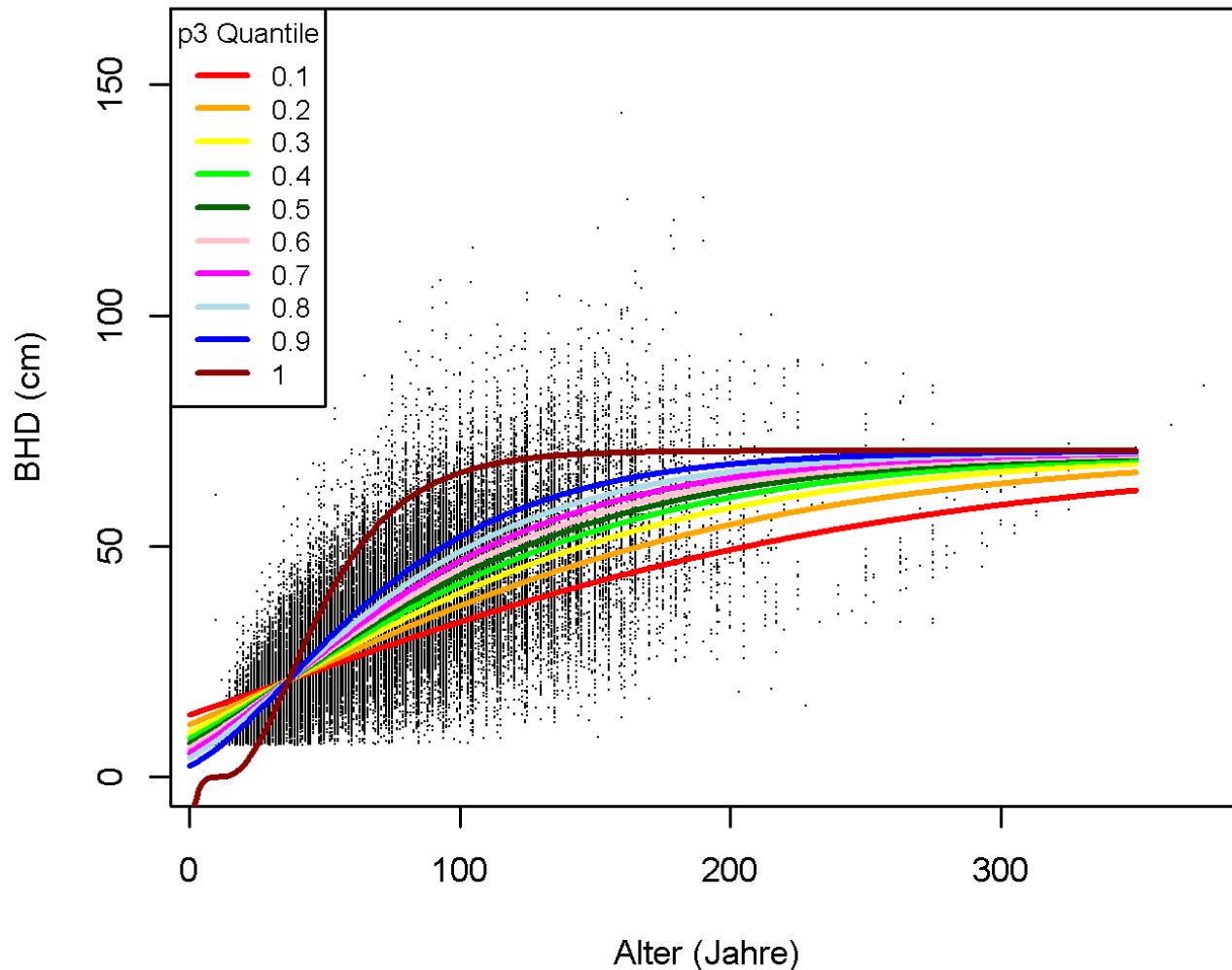
# Curves of the quantiles of the BLUP for p1 (asymptote (cm))



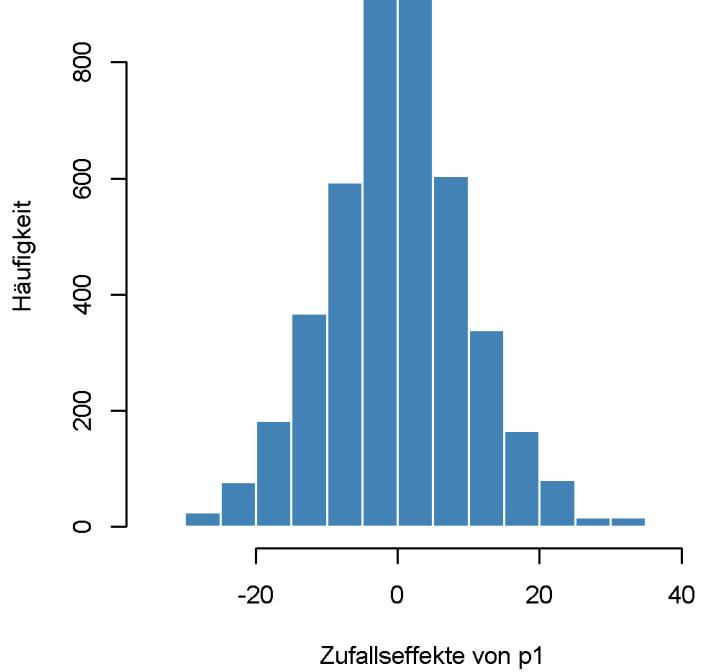
# Curves of the quantiles of the BLUP for p2 (point in time of maximum diameter growth (a))



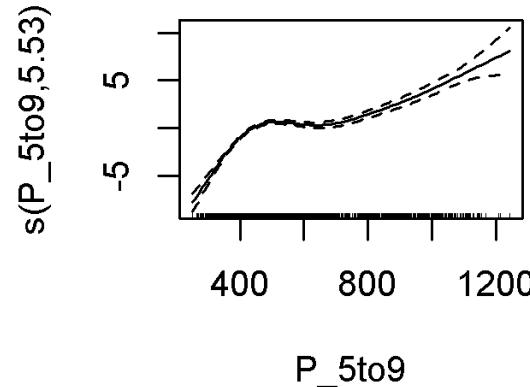
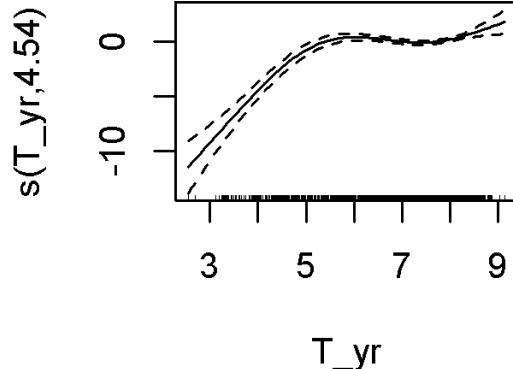
# Curves of the quantiles of the BLUP for p3 (maximum diameter growth (cm/a))



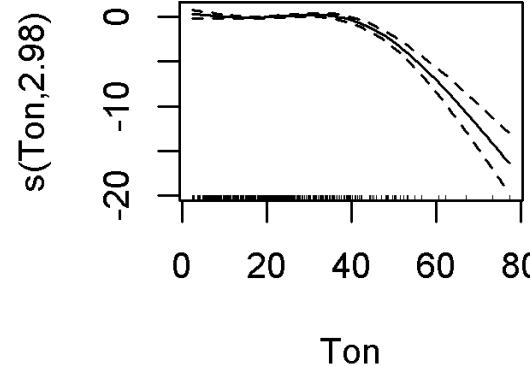
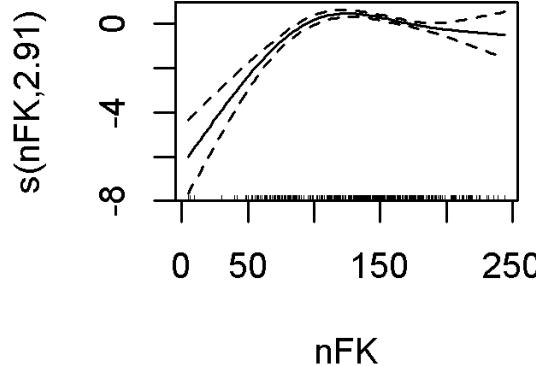
# Random effects of p1



# Effects of environmental variables on random parameter p1

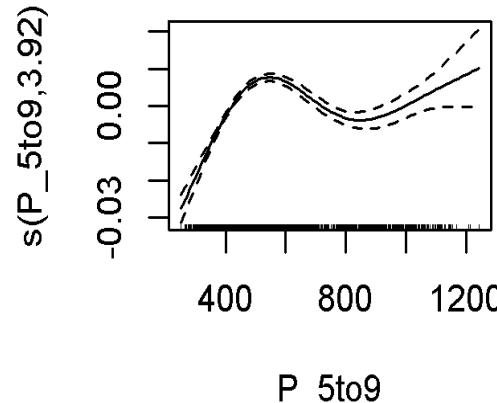
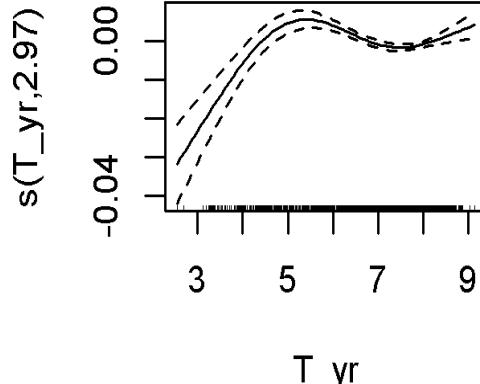


$T_{yr}$ : Jahresmitteltemperatur  
 $P_{5to9}$ : Niederschlagssumme von Mai bis September  
nFK: nutzbare Feldkapazität

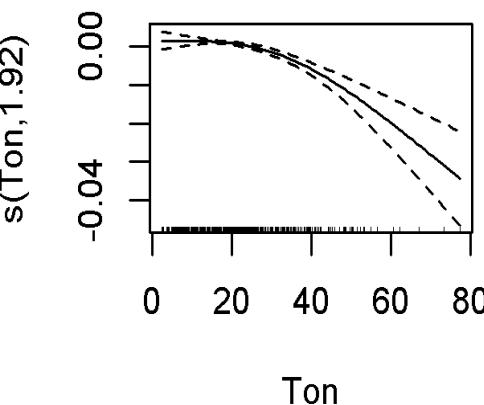
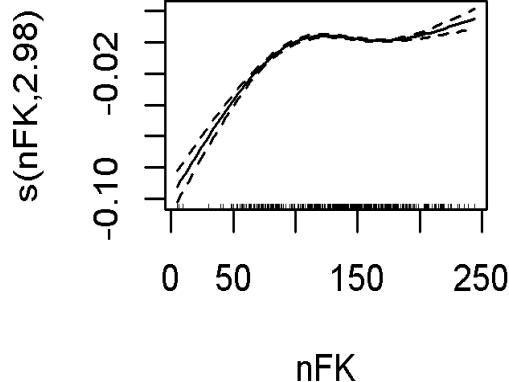


$R^2 = 4.12 \%$

# Effects of environmental variables on random parameter p3



$T_{\text{yr}}$ : Jahresmitteltemperatur  
 $P_{\text{5to9}}$ : Niederschlagssumme von Mai bis September  
nFK: nutzbare Feldkapazität



$R^2 = 3.75 \%$

# Integration of environmental effects in the Bertalanffy-Model

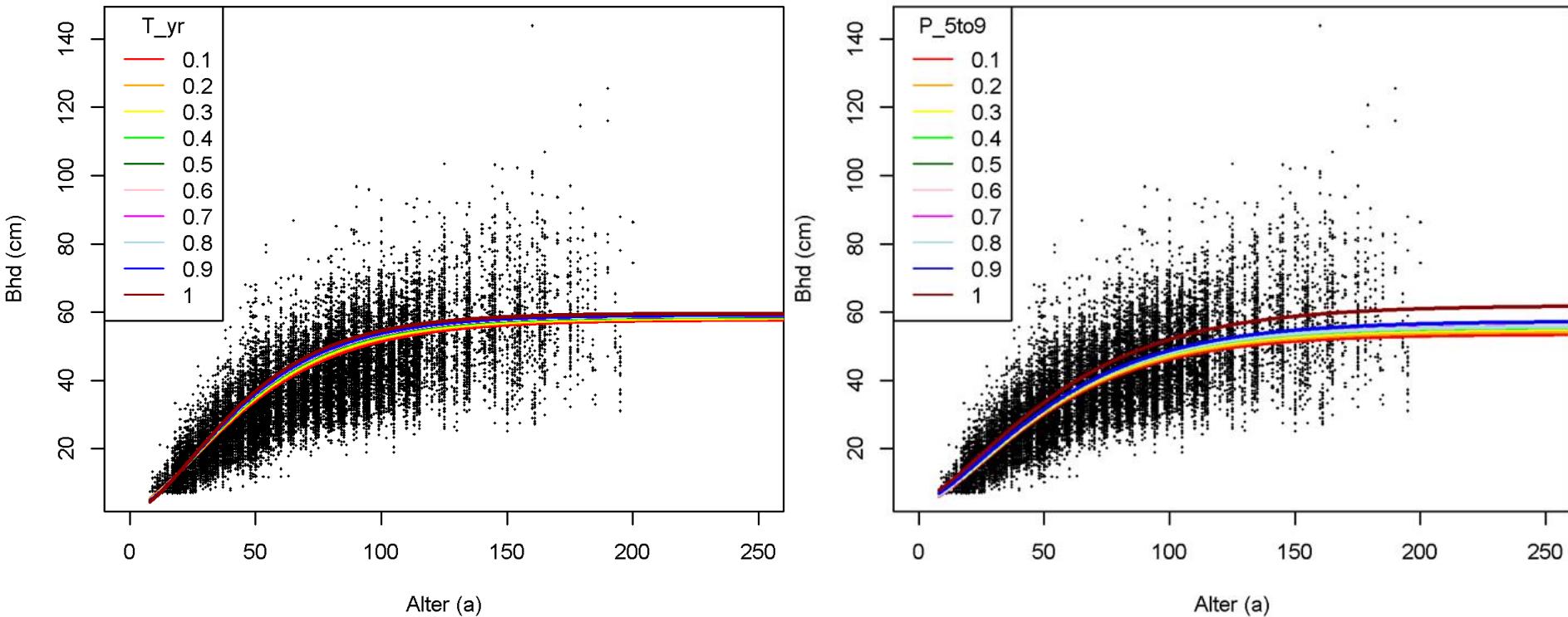
## ■ Reestimation of the model parameters

$$BHD_{ijk} = p_{1i} \cdot \left( 1 - \frac{1}{3} \cdot e^{\left( \frac{p_{3i} \cdot (p_2 - Alter_{ijk})}{p_{1i}} \cdot \frac{9}{4} \right)} \right)^3$$

$$p_1 = \alpha_{0i} + \alpha_1 \cdot s_{T_{yr}} + \alpha_2 \cdot s_{P_{5to9}} + \alpha_3 \cdot s_{nFK} + \alpha_4 \cdot s_{Ton}$$

$$p_3 = \beta_{0i} + \beta_1 \cdot s_{T_{yr}} + \beta_2 \cdot s_{P\_5to9} + \beta_3 \cdot s_{nFK} + \beta_4 \cdot s_{Ton}$$

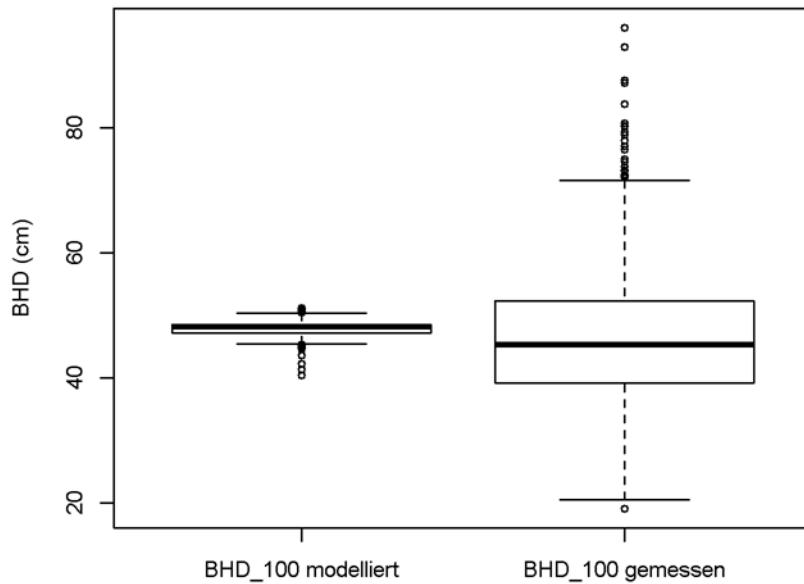
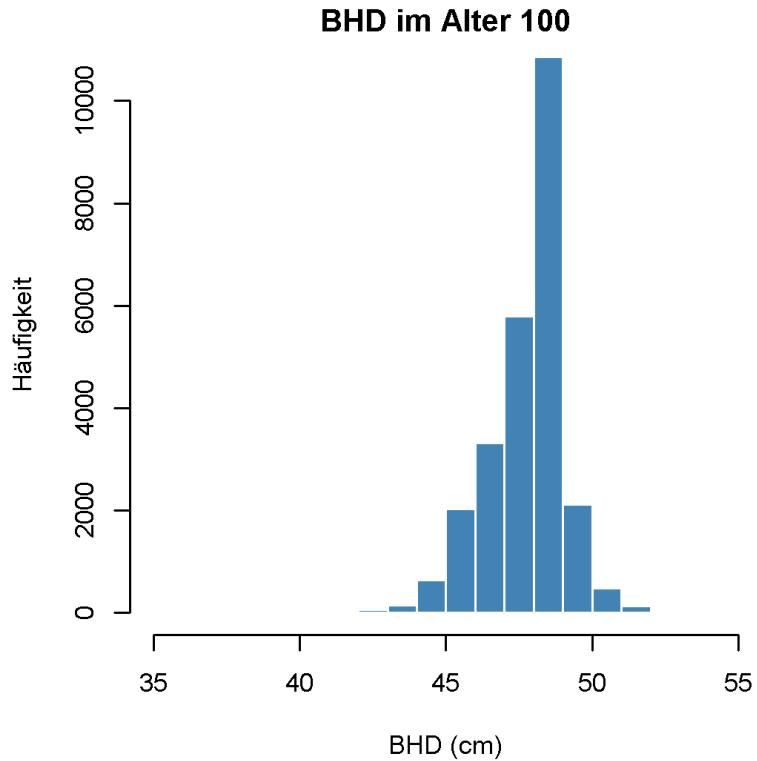
# Effect of temperature and precipitation on diameter-age-model



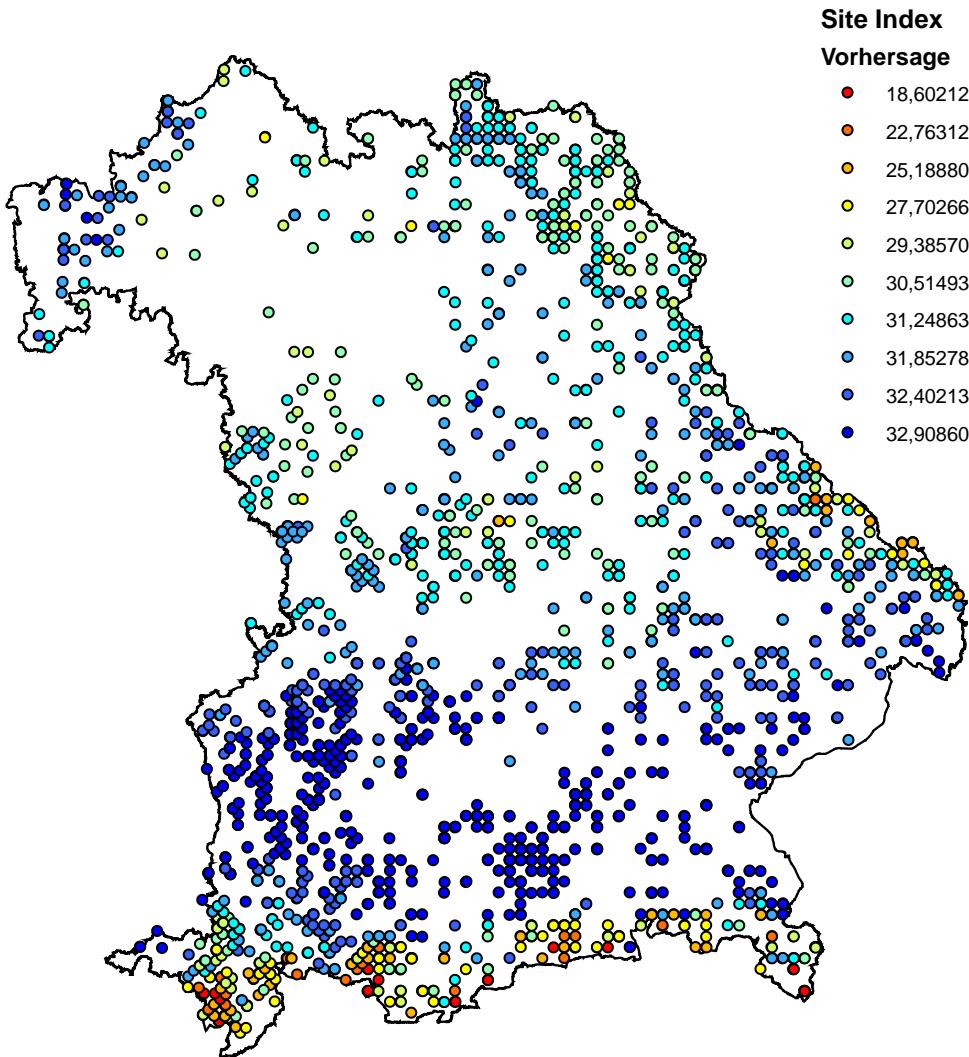
T\_yr: Jahresmitteltemperatur

P\_5to9: Niederschlagssumme von Mai bis September

# Predicted diameters at age 100 (only fixed effects)



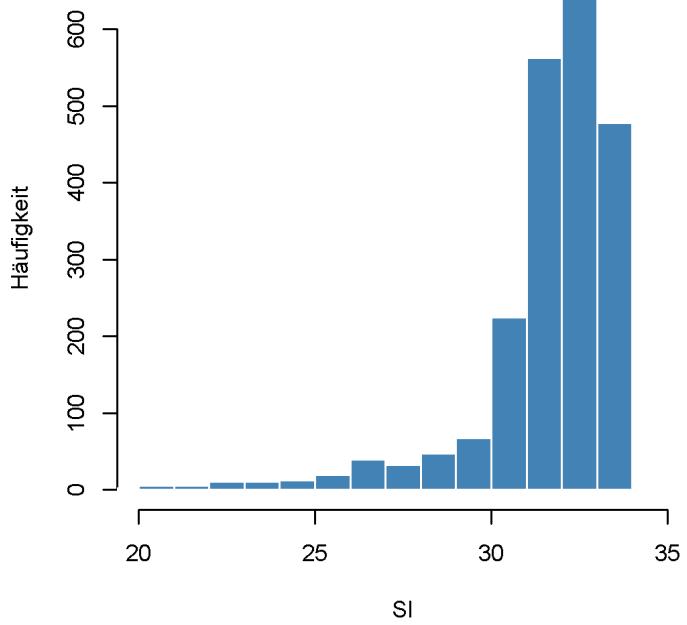
# Site Index Predictions



## Site Index

### Vorhersage

- 18,602129 - 22,763127
- 22,763128 - 25,188802
- 25,188803 - 27,702663
- 27,702664 - 29,385707
- 29,385708 - 30,514932
- 30,514933 - 31,248633
- 31,248634 - 31,852787
- 31,852788 - 32,402137
- 32,402138 - 32,908603
- 32,908604 - 33,567999



# Method: Combining two models

## ■ diameter-age-Model

- Bertalanffy function
- Response: DBH
- Target variable: DBH at age 100 = input variable for height-diameter-model

## ■ height-diameter-Model

- Korf function
- Response: height
- Target variable: height at age 100 = Site Index

# Reasons for modeling in two steps

- Height as response variable and measure for site potential as it is less affected by management than diameter
  - Why not modeling the relationship between height and age? (instead of first modeling the relationship between height and diameter and then the relationship between diameter and age)
    - The relationship between height and diameter is better than the relationship between height and age, because trees of the same age can differ very much in height
    - DBH is measured quite exactly for all trees, whereas age is a rough estimation
- > main model: height-diameter-model
- Not only height but also diameter depends on environmental conditions

# Next steps

- Focus on environmental variables -> better explanatory variables
- Integrating interactions
- Allowing for management effects in Diameter-Age-Model
- Direct calculation of SI from BWI-data and subsequent use as response variable in a regression model with environmental conditions as explanatory variables (Nothdurft et al. 2012)
  - > comparison of the results